

Jucied Log

Description

Now, you are solving a problem about sequence.

Given a list of N integers a_1, a_2, \dots, a_N and Q operations, each operation is one of the following:

- 1 $L R e$: $\forall i \in [L, R]$, change a_i to $\lfloor \log_e a_i \rfloor$. Note that, if a_i is 0, then $\lfloor \log_e a_i \rfloor = 0$
- 2 $x y$: change a_x to y .
- 3 $L R$: please calculate $\sum_{i=L}^R \sum_{j=i+1}^R \sum_{k=j+1}^R a_i a_j a_k \mod (10^9 + 9)$

Input

The first line of the input contains two integers N, Q .

The second line contains N space-separated integers a_1, a_2, \dots, a_N .

Then, there are Q lines, each line contains one operation. The format of the operation is mentioned in the description above.

- $1 \leq N, Q \leq 2 \times 10^5$
- $0 \leq a_i, y \leq 10^9$
- $1 \leq L \leq R \leq N$
- $1 \leq x \leq N$
- $2 \leq e \leq 10^9$

All numbers in the input are integers.

Output

For operation 3, output the corresponding result.

Sample Input

```
4 6
2 3 4 5
3 1 4
2 2 100
3 1 3
1 1 4 2
3 1 3
3 4 4
```

Sample Output

```
154
800
12
0
```